

**Final exam DITE:** Tuesday, January 8, 2013 -- 14:00 to 17:00h

**Task I:** Convert the following numbers from the given base to the other listed bases in the table.

| Decimal | Binary       | Octal | Hexadecimal |
|---------|--------------|-------|-------------|
| 10.3125 | ?            | ?     | ?           |
| ?       | 11100101.101 | ?     | ?           |
| ?       | ?            | 623.5 | ?           |
| ?       | ?            | ?     | A4D7.C      |

**Important:** Show and explain the conversion procedures you use and not only the final result.

**Task II:** A combinational circuit is defined by the following three Boolean functions:

$$F1 = (X+Z)' + XYZ$$

$$F2 = (X+Z)' + X'YZ$$

$$F3 = (X+Z)' + XY'Z$$

Implement the circuit using two 2-to-4 Decoders with enable and external NAND gates.

**Task III:** Simplify the Boolean function  $F(W,X,Y,Z) = \sum m(1,2,4,5,6,8,9)$  which has the don't-care conditions  $d(W,X,Y,Z) = \sum m(10,11,14,15)$  by finding all prime implicants and essential prime implicants and applying the selection rule. Note that function **F** has *don't care* conditions **d** that you have to take into account when simplifying function **F**. After you have simplified the function, represent it using the **logic basis NOR**. Also, draw the combinational logic circuit corresponding to the function **using only 2-input NOR gates**.

**Important:** Show all prime implicants and essential prime implicants as well as explain all the steps you do to simplify and represent function **F**.

**Task IV:** A sequential circuit with two flip-flops A and B, one input X, and one output Z is specified by the following equations:

$$A(t+1) = X(t)'A(t) + X(t)B(t)$$

$$B(t+1) = X(t)'A(t)'$$

$$Z(t) = X(t)A(t) + X(t)B(t)'$$

Implement the circuit described above as **Moore Finite State Machine (FSM)** under the following conditions:

1. Use **only** NAND gates and T Flip-Flops;
2. Derive and show the state table of the Moore FSM;
3. Derive and show the state diagram of the Moore FSM;
4. Draw the logic diagram of the Moore FSM.

**Important:** Show and explain all the steps you do to implement the circuit above.